

Lesson 6.2: Reverse Chain Rule & u-Substitution

Warm Up:

Differentiate:

1. $\frac{d}{dx}(1 + 5x)^4 =$

2. $\frac{d}{dx}\sin(1 + 5x) =$

Integrate:

3. $\int 5(1 + 5x)^3 dx =$

4. $\int 5 \cos(1 + 5x) dx =$

Note: You “hooked on” the derivative of the _____ in Examples 1 and 2, so you had to “unhook” the derivative of the inside function in Examples 3 and 4.

Rule	x Form	u Form (Reverse Chain Rule)
Power Rule		
Trig Rules	$\int \cos(x) dx =$	
	$\int \sin(x) dx =$	
	$\int \sec^2(x) dx =$	
	$\int \csc^2(x) dx =$	
	$\int \sec(x) \tan(x) dx =$	
	$\int \csc(x) \cot(x) dx =$	

Examples: Integrate.

1. $\int (3x - 1)^{10} dx$

2. $\int (3t^2 + 2t)(t^3 + t^2) dt$

3. $\int \frac{6x^2}{\sqrt{4x^3 - 5}} dx$

4. $\int (y^3 + 1)^2 dy$

5. $\int \sin(4x) dx$

6. $\int 3\theta \cos(\theta^2) d\theta$

7. $\int \sin^2(x) \cos(x) dx$

u-Substitution

For more complicated integration problems, simple rules for integration might fail and you may have to make some type of substitution to be able to integrate.

Procedure:

1	
2	
3	
4	
5	

Examples: Integrate.

1. $\int x\sqrt{x-1}dx$

2. $\int \frac{2x-1}{\sqrt{2x+3}} dx$

3. $\int \frac{\sin(3x)}{\sqrt{5+\cos(3x)}} dx$

4. $\int (\sin^2(x))(\cos(x))dx$

